# Air Resistance 

A Variable Force...

## Dynamics

I. Newton's 3 Laws of Motion

- inertia, force, mass, weight
- interaction \& nature of force
II. Normal Force
III. Compression, Tension, Sections
IV. Pulleys and Systems
V. Friction (between solids)
VI. Air Resistance
VII. Inclines, ramps, etc.

|  | The student will be able to: | HW: |
| :---: | :--- | :--- |
| 1 | State Newton's 1st and 2nd <br> situations in order to determine of Motion and apply these laws to physical <br> object's sesulting behavior. Define and apply the concept of inertia and <br> inertial frame of reference. |  |

Which object would experience the greatest amount of air resistance when falling?

How would the speeds compare when falling?


Weight:
1 N
1 N
4 N

## Diameter:

10 cm
20 cm
20 cm

A falling object accelerates and gains speed as long as the downward pull of gravity (weight) is greater than the air resistance (drag). However, because drag increases with speed, eventually there is enough air resistance to perfectly balance the pull of gravity and cause the acceleration to be zero - this is the terminal velocity state.

## Air resistance $=1 \mathbf{N}$

For a relatively lightweight object there will be a relatively low terminal velocity because not too much air resistance is
Weight $=1 \mathrm{~N}$ required to prevent acceleration.

## Terminal velocity $=\mathbf{8} \mathbf{~ m} / \mathrm{s}$

## Twice the diameter as previous...

With twice the diameter there is four times the cross-sectional area as the previous, increasing the drag by factor four at a given speed. Terminal velocity occurs at half the speed as before because drag is most closely proportional to the square of the speed.


With weight unchanged from the previous the amount of air resistance at terminal velocity would be the same as before. However, this amount of drag occurs at a lower speed.

## Terminal velocity $=4 \mathrm{~m} / \mathrm{s}$

## Quadruple the weight as the previous...

With twice the pull of gravity as the previous the object must fall faster through the air to produce enough drag to prevent acceleration.

## Air resistance $=4 \mathbf{N}$

Weight $=4 \mathrm{~N}$
At twice the speed through the air as previous there would be approximately four times the drag. This object would have the same terminal velocity as the smallest object in this example set of three. But, it would experience four times the amount of air resistance.

## Terminal velocity $=\mathbf{8} \mathbf{~ m} / \mathrm{s}$

## Modeling Motion through Air

- Air resistance is often ignored and acceleration is assumed constant $9.8 \mathrm{~m} / \mathrm{s}^{2}$ downward - the object is said to be in "freefall"
- In reality, air resistance depends on speed, crosssectional area, density of the air, and the aerodynamic shape (i.e. how "streamlined").
- Usually it is assumed that air resistance is proportional to speed or that it is proportional to the square of the speed. Although neither assumption is exactly correct, the latter is usually more accurate especially at higher speeds.
- Air resistance is directly proportional to crosssectional area and density of air.


## Modeling Motion through Air

- The graphs that follow illustrate the kinematics of objects moving through the air based on the three different modeling approaches.
- The red lines/curves represent freefall.
- The blue curves represent air resistance proportional to speed squared (and best represent reality in most situations).
- The green curves represent air resistance proportional to speed (a common approach used in physics to approximate reality).


## Position vs. Time for a Skydiver


initial velocity $=$ zero; terminal speed $=55 \mathrm{~m} / \mathrm{s}$


|  | drag | net force | acceleration | speed |
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| $\mathrm{t}=0 \mathrm{~s}$ | 0 | 800 N | 9.8 m/ ${ }^{2}$ | 0 |
| $\mathrm{t}=2 \mathrm{~s}$ | 80 N | 720 N | $8.7 \mathrm{~m} / \mathrm{s}^{2}$ | $19 \mathrm{~m} / \mathrm{s}$ |
| $\mathrm{t}=4 \mathrm{~s}$ | 290 N | 510 N | $6.2 \mathrm{~m} / \mathrm{s}^{2}$ | $34 \mathrm{~m} / \mathrm{s}$ |
| $\mathrm{t}=6 \mathrm{~s}$ | 500 N | 300 N | $3.7 \mathrm{~m} / \mathrm{s}^{2}$ | $44 \mathrm{~m} / \mathrm{s}$ |
| $\mathrm{t}=8 \mathrm{~s}$ | 640 N | 160 N | 2.0 m/s ${ }^{2}$ | $49 \mathrm{~m} / \mathrm{s}$ |
| $\mathrm{t}=10 \mathrm{~s}$ | 718 N | 82 N | 1.0 m/s ${ }^{2}$ | $52 \mathrm{~m} / \mathrm{s}$ |
| $\mathrm{t}=12 \mathrm{~s}$ | 757 N | 43 N | $0.53 \mathrm{~m} / \mathrm{s}^{2}$ | $53 \mathrm{~m} / \mathrm{s}$ |
| $\mathrm{t}=14 \mathrm{~s}$ | 779 N | 21 N | $0.26 \mathrm{~m} / \mathrm{s}^{2}$ | $54 \mathrm{~m} / \mathrm{s}$ |
| $\mathrm{t}=16 \mathrm{~s}$ | 789 N | 11 N | $0.13 \mathrm{~m} / \mathrm{s}^{2}$ | $55 \mathrm{~m} / \mathrm{s}$ |
| $\mathrm{t}=18 \mathrm{~s}$ | 795 N | 5 N | $0.06 \mathrm{~m} / \mathrm{s}^{2}$ | $55 \mathrm{~m} / \mathrm{s}$ |

## Position vs. Time for a Skydiver


initial velocity $=$ zero; terminal speed $=55 \mathrm{~m} / \mathrm{s}$

## Velocity vs. Time for a Skydiver


initial velocity $=$ zero; terminal speed $=55 \mathrm{~m} / \mathrm{s}$

Acceleration vs. Time for a Skydiver

initial velocity $=$ zero; terminal speed $=55 \mathrm{~m} / \mathrm{s}$

Note that the terminal velocity of a skydiver can be different depending on how he is falling: when "spread eagle" the cross-sectional area is maximized \& terminal speed is about 120 mph .

## Drag $=800$ N

## Weight $=\mathbf{8 0 0} \mathrm{N}$

## Terminal velocity $=\mathbf{5 5} \mathbf{~ m} / \mathrm{s}$

Note that the terminal velocity of a skydiver can be different depending on how he is falling: if "diving" head first the cross-sectional area is minimized \& terminal speed is about 170 mph .

## Drag $=800$ N

## Weight $=\mathbf{8 0 0} \mathbf{N}$

## Terminal velocity $=75 \mathrm{~m} / \mathrm{s}$



## Weight $=800 \mathrm{~N}$

## Terminal velocity $=\mathbf{5} \mathbf{~ m} / \mathrm{s}$

## Position vs. Time for a Baseball


initial velocity $=20 \mathrm{~m} / \mathrm{s}$, upward; terminal speed $=45 \mathrm{~m} / \mathrm{s}$

## Velocity vs. Time for a Baseball

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initial velocity $=20 \mathrm{~m} / \mathrm{s}$, upward; terminal speed $=45 \mathrm{~m} / \mathrm{s}$

## Acceleration vs. Time for a Baseball

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initial velocity $=20 \mathrm{~m} / \mathrm{s}$, upward; terminal speed $=45 \mathrm{~m} / \mathrm{s}$

## Position vs. Time for a Balloon


initial velocity $=8 \mathrm{~m} / \mathrm{s}$, upward; terminal speed $=3 \mathrm{~m} / \mathrm{s}$

## Velocity vs. Time for a Balloon

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initial velocity $=8 \mathrm{~m} / \mathrm{s}$, upward; terminal speed $=3 \mathrm{~m} / \mathrm{s}$

## Acceleration vs. Time for a Balloon


initial velocity $=8 \mathrm{~m} / \mathrm{s}$, upward; terminal speed $=3 \mathrm{~m} / \mathrm{s}$

## Position vs. Time for a Balloon


initial velocity $=8 \mathrm{~m} / \mathrm{s}$, downward; terminal speed $=3 \mathrm{~m} / \mathrm{s}$

## Velocity vs. Time for a Balloon

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initial velocity $=8 \mathrm{~m} / \mathrm{s}$, downward; terminal speed $=3 \mathrm{~m} / \mathrm{s}$

## Acceleration vs. Time for a Balloon


initial velocity $=8 \mathrm{~m} / \mathrm{s}$, downward; terminal speed $=3 \mathrm{~m} / \mathrm{s}$

## Generic Exponential Curve



Generic Exponential Curve


The "time constant" $\tau$ is often used as a convenient way to analyze exponential functions. Using the model that drag $=\mathrm{kv}$ it can be shown that the time constant is given by $\tau=m / k$. For the particular case of a falling object the time constant can also be found by $\tau=v_{\mathrm{t}} / g$.

| Falling Object |  |  |
| :---: | :---: | :---: |
| time | speed | acceleration |
| 0 | $0 \% v_{\mathrm{t}}$ | $100 \% \mathrm{~g}$ |
| $1 \tau$ | $63 \% v_{\mathrm{t}}$ | $37 \% \mathrm{~g}$ |
| $2 \tau$ | $86 \% v_{\mathrm{t}}$ | $14 \% \mathrm{~g}$ |
| $3 \tau$ | $95 \% v_{\mathrm{t}}$ | $5 \% \mathrm{~g}$ |
| $4 \tau$ | $98 \% v_{\mathrm{t}}$ | $2 \% \mathrm{~g}$ |
| $5 \tau$ | $99 \% v_{\mathrm{t}}$ | $1 \% \mathrm{~g}$ |

