

Work and Energy

- I. Work
 - dot product
 - varying force
- II. Work-Energy Theorem
 - Kinetic Energy
- III. Potential Energy
 - Conservative Forces
- IV. Machines, Power, Efficiency**

	The student will be able to:	HW:
1	Define and apply the concept of work (and the joule) for constant or varying force and solve related problems.	✓ 1 – 9
2	Define and apply kinetic energy. State and apply the work-energy theorem and solve related problems.	✓ 10 – 15
3	Solve problems using conservation of mechanical energy, including situations involving nonconservative forces.	✓ 16 – 23
4	Solve problems involving gravitational potential energy in which g is not taken to be constant.	✓ 24 – 26
5	Solve problems involving work and energy for a mass attached to a spring.	✓ 27 – 29
6	Define and apply the concepts of conservative force and potential energy and solve related problems.	✓ 30 – 32
7	Define and apply the concept of power (and the watt) and solve related problems.	33 – 37
8	Solve problems involving machines and efficiency.	38 – 40

Power

Power is the rate at which work is done (or the rate of energy transfer/transformation):

$$P = \frac{dW}{dt}$$

where: $W =$ work
 $t =$ time

Units of measure:

$$1 \text{ watt} = 1 \text{ joule} \div 1 \text{ second}$$

$$W = \text{J/s}$$

$$W = \text{kg m}^2/\text{s}^3$$

$$1 \text{ horsepower (hp)} \approx 746 \text{ W}$$

Power

The **instantaneous power** of a particular force acting on an object equals the dot product of force and the object's velocity:

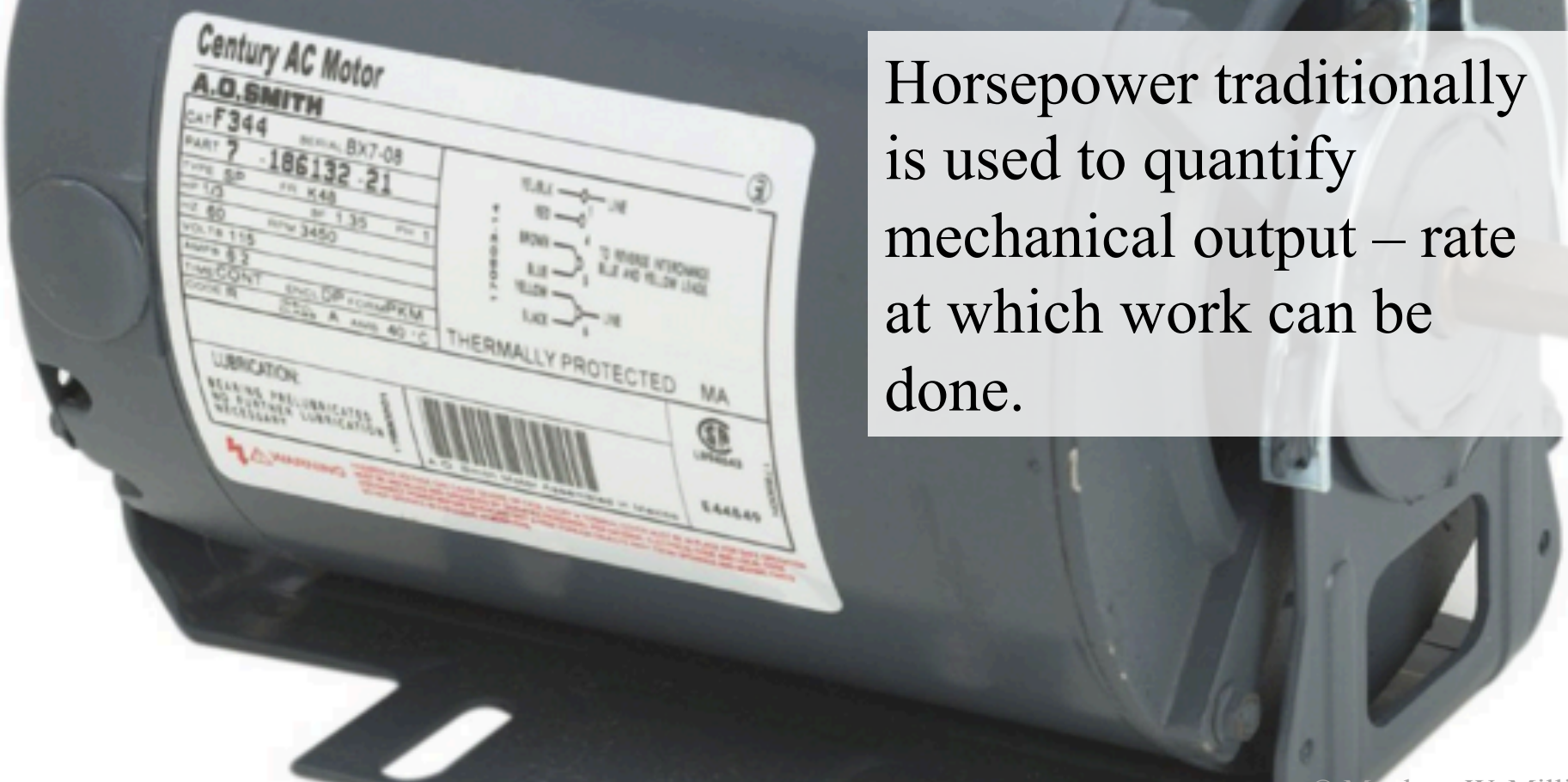
$$P = \vec{F} \cdot \vec{v}$$

This result may be derived from the definitions of work and velocity.



On an electrical device the number of watts typically indicates the power input – rate of energy usage.

Horsepower traditionally is used to quantify mechanical output – rate at which work can be done.



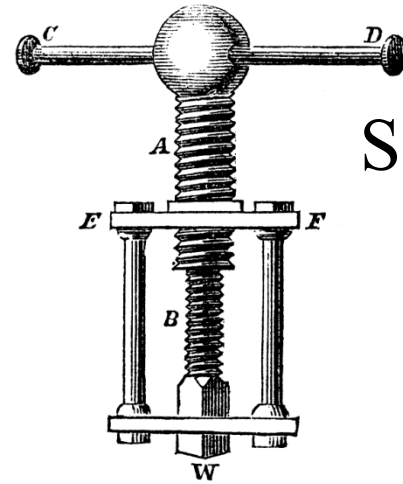
Simple Machines



Inclined Plane



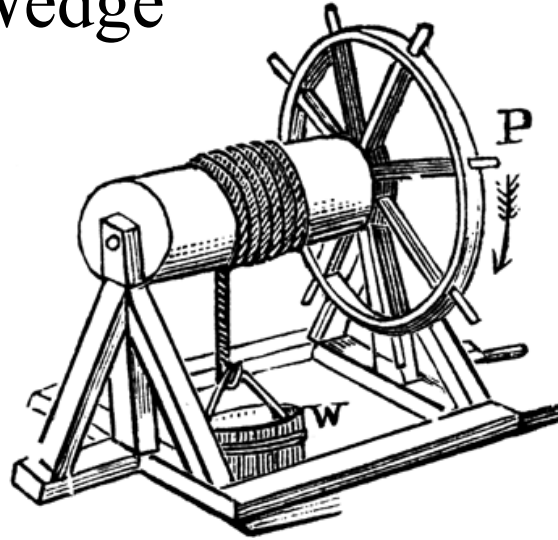
Wedge



Screw



Lever



Wheel and Axle



Pulley

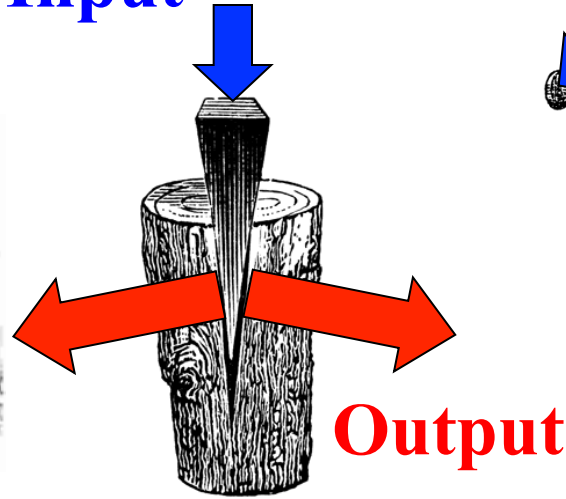
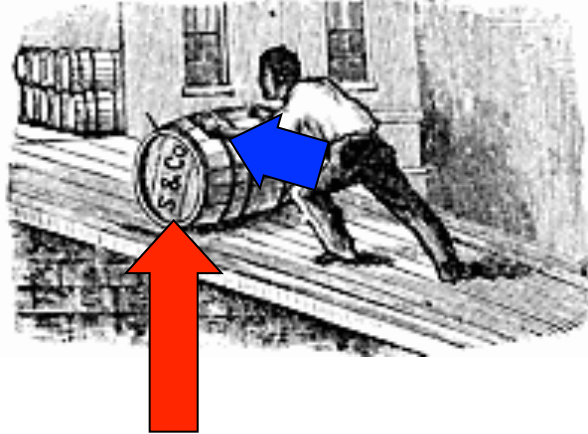
Simple Machines

All simple machines are "force multipliers" that can make a task easier to accomplish.

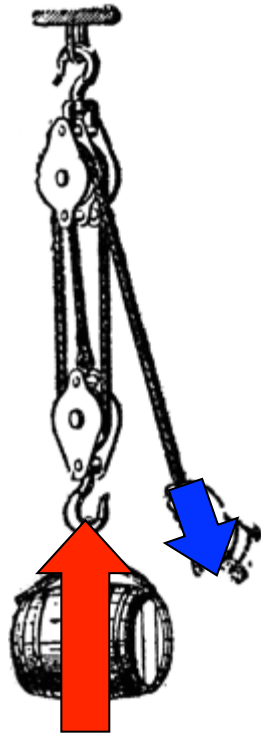
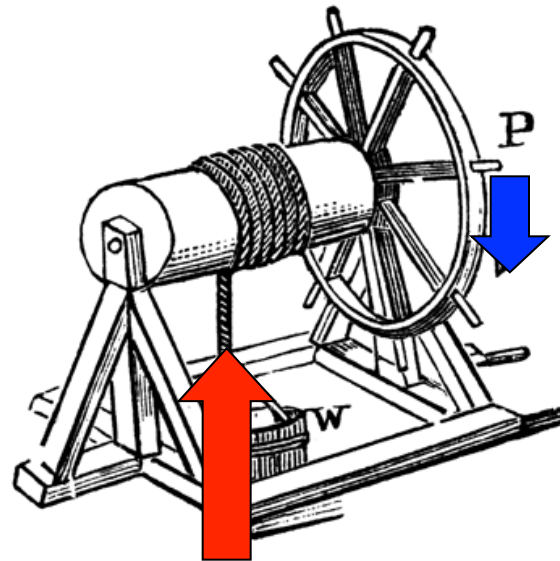
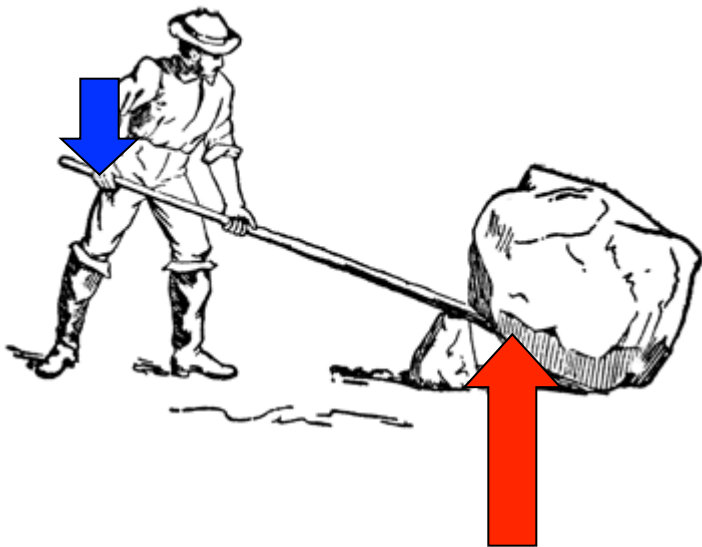
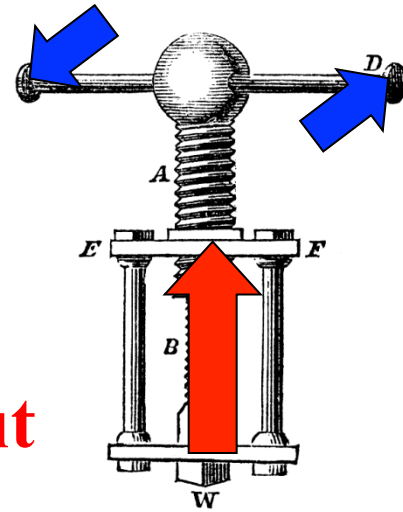
Although a machine may provide an increased force it cannot violate conservation of energy.

The work (or energy) output of a machine cannot exceed the work (or energy) put into it.

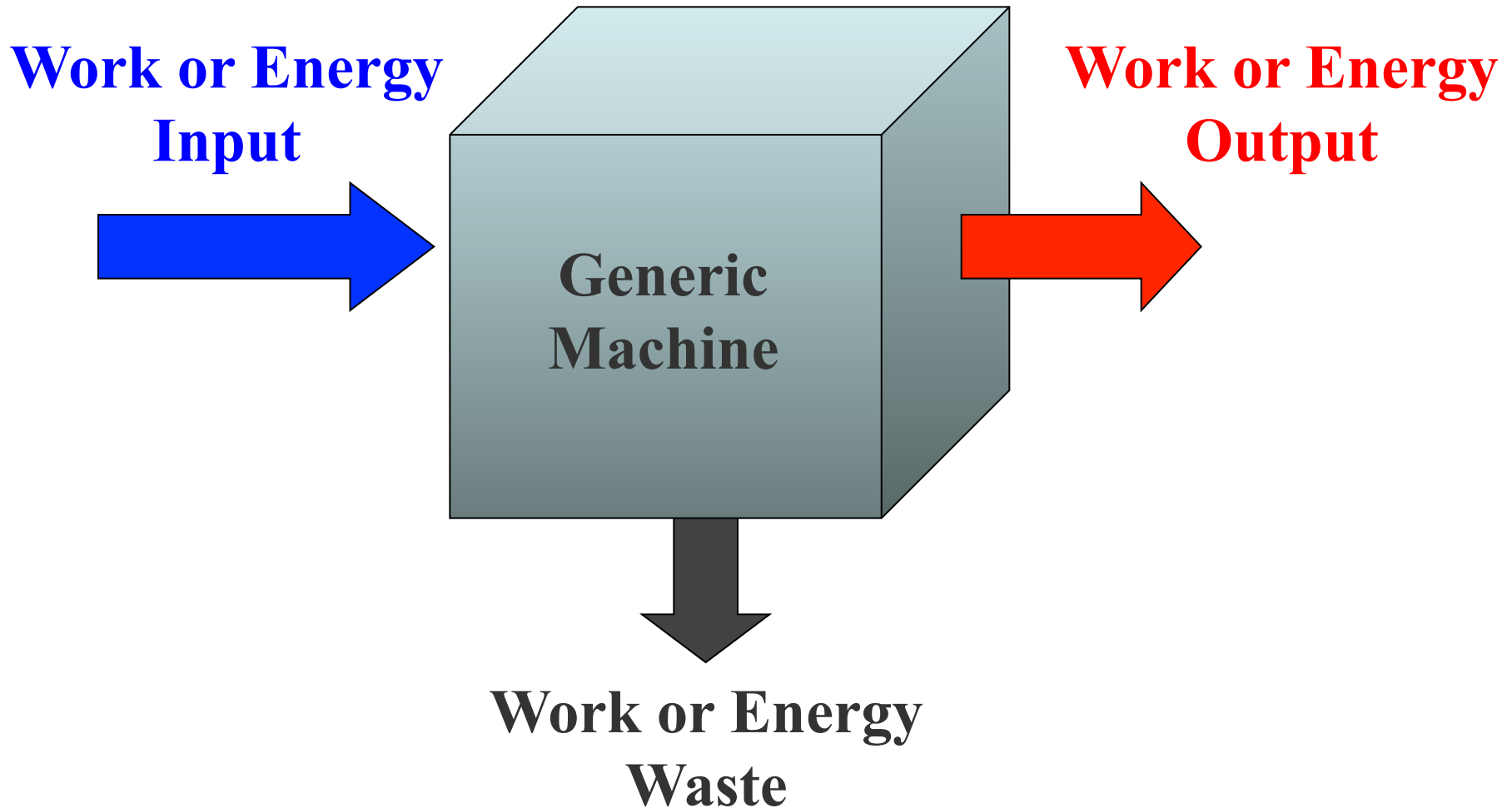
Input



Output



Efficiency



Efficiency

Efficiency is the amount of useful output relative to the input, usually expressed as a percentage.

$$\textit{efficiency} = \frac{\textit{useful output}}{\textit{input}}$$