# Magnetic Induction

- I. Induction
  - Faraday's Law, Lenz's Law

II. Maxwell's equations

III.Inductance and Inductors

- design and geometry

**IV.RL** Circuits

- steady state, dynamic behavior

V. LC Circuits - oscillations

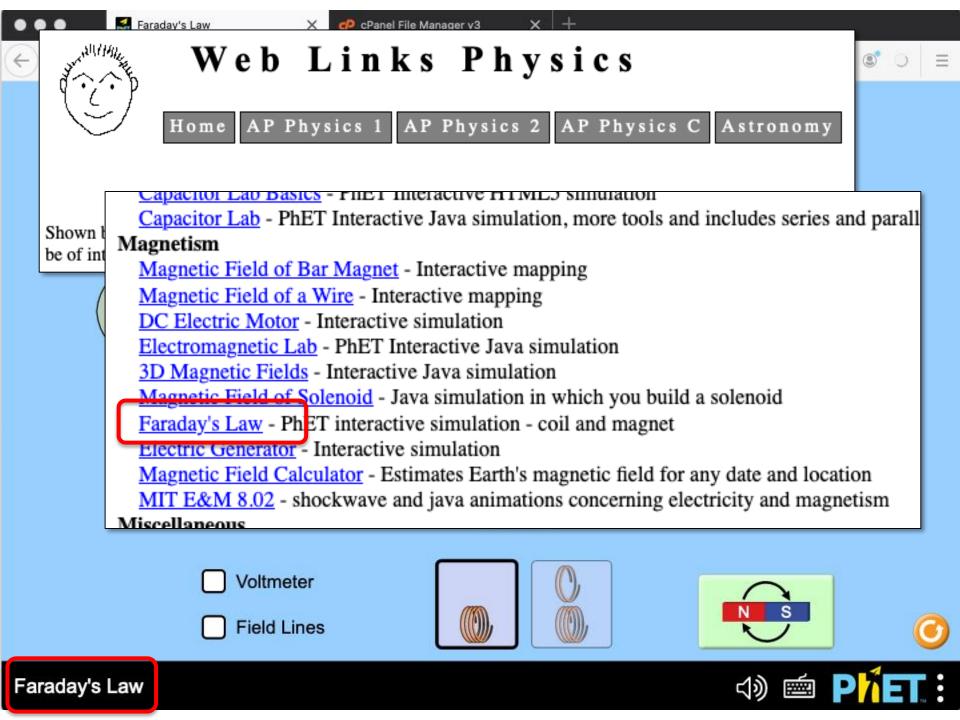
### Magnetic Induction

#### Faraday's Law, Lenz's Law

	The student will be able to:	HW:
1	State and apply Faraday's Law and Lenz's Law and solve magnetic induction problems involving changing magnetic flux, and induced emf or eddy currents.	1 – 16
2	Solve problems involving basic principles of generators, including production of back emf.	17 – 21
3	State and recognize Maxwell's equations and associate each equation with its implications.	22-23
4	Define and calculate inductance and solve related problems including those that involve parallel or series inductors.	24 – 31
5	Analyze RL circuits in terms of the appropriate differential equation and resulting exponential functions for charge, current, voltage, etc.	32 - 38
6	Analyze LC and RLC circuits in terms of the appropriate differential equation and resulting exponential functions for charge, current, voltage, etc.	39 – 41

### Induction

• Just as an electric field can induce an electrostatic charge, a magnetic field can induce a current.



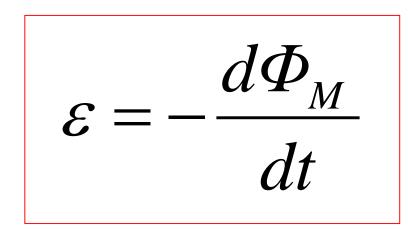
## Questions to Explore

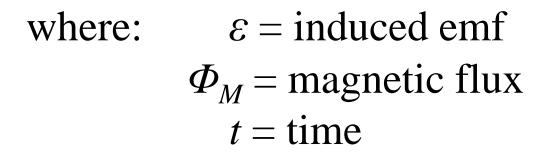
- How does the motion of the magnet affect the electricity generated what produces the greatest current and voltage?
- What determines the direction of current?
- Is there any position at which magnet produces electricity if it is not moving?
- Is there any position at which the magnet produces no electricity if it is moving?
- What is the effect of having more turns in the coil? Look closely at how circuit is wired.

## Induction

- Just as an electric field can induce an electrostatic charge, a magnetic field can induce a current.
- However, it is observed that only a *changing* magnetic field can result in a current presence of a *static* magnetic field will <u>not</u> induce a current.
- If current exists, it follows that there must be voltage, which in this case is called emf ("electromagnetic force").

# Faraday's Law



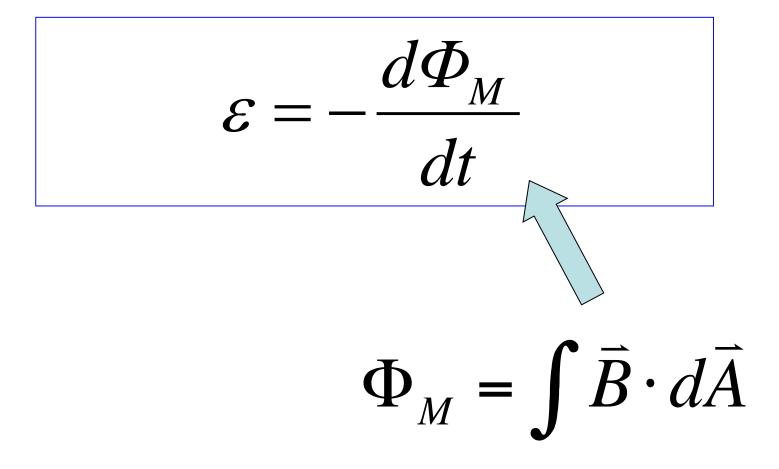


### Magnetic Flux

$$\phi_{M} = \int \vec{B} \cdot d\vec{A}$$

where: 
$$\Phi_M$$
 = magnetic flux  
 $B$  = magnetic field  
 $A$  = area

#### SI unit: 1 weber = 1 tesla $\cdot$ 1 meter<sup>2</sup> Wb = T $\cdot$ m<sup>2</sup>



 $\varepsilon = -\frac{d}{dt} \int \vec{B} \cdot d\vec{A}$ 

The magnet moving to the left is causing an increase in magnetic flux. This induces a current and an emf clockwise when facing the approaching magnet.

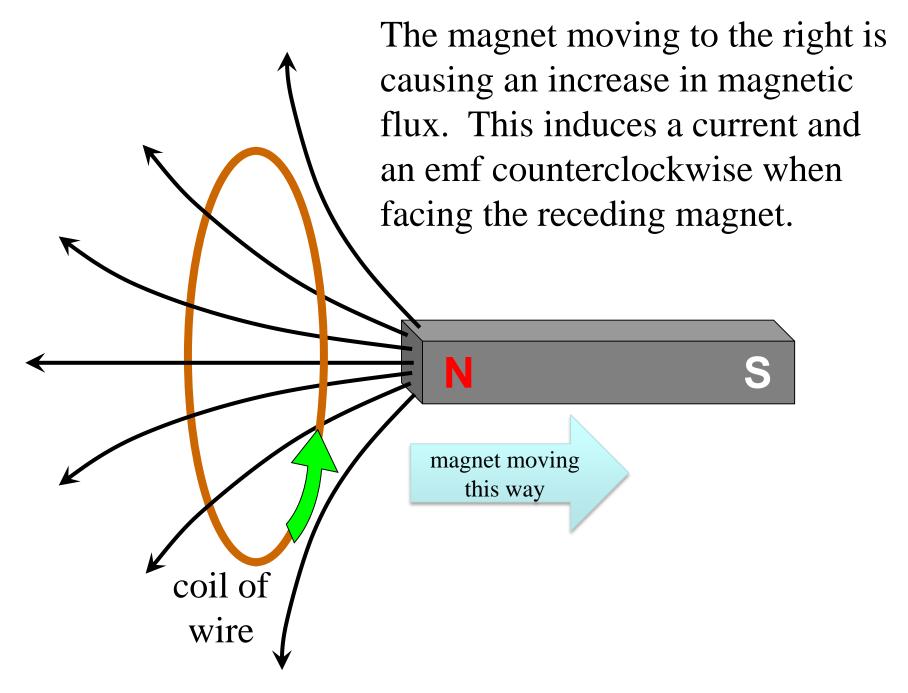
Ν

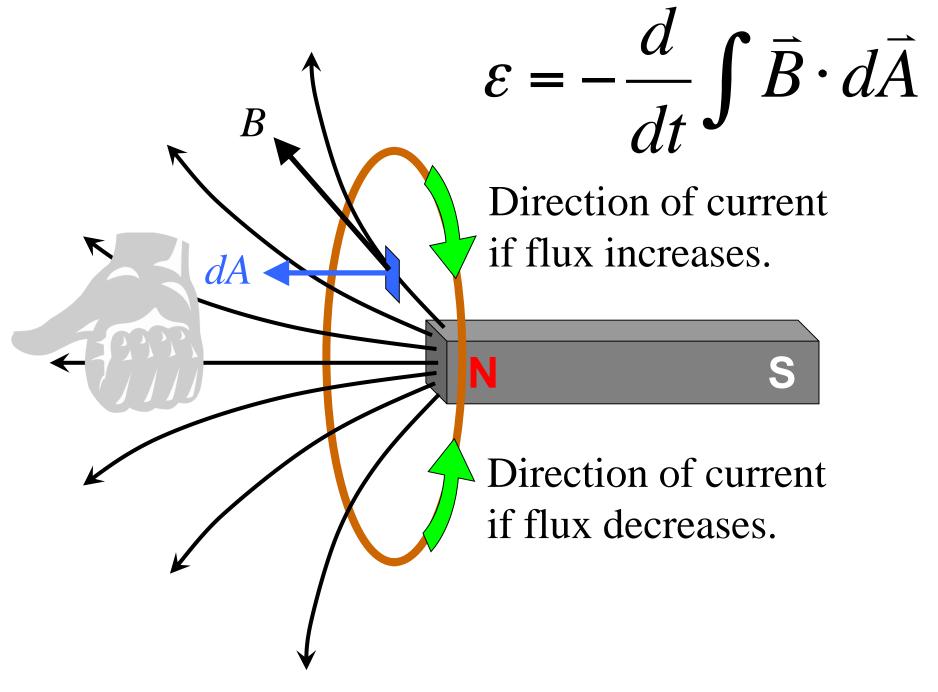
coil of

wire

magnet moving

this way



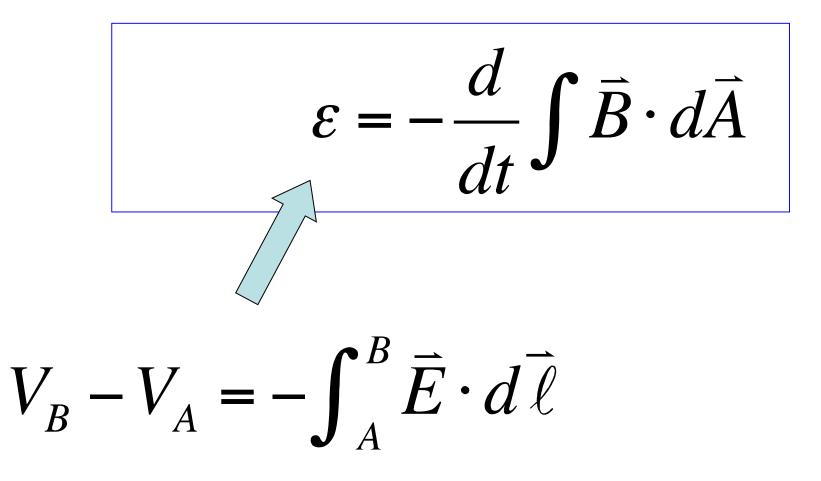


## About the Induced EMF

- The negative sign in Faraday's Law indicates the sense of the induced emf.
- The direction in which this emf drives current is referred to as the "sense" of the emf.
- Unlike other voltage sources, an induced emf is not the potential difference between two points (like the terminals of a battery).
- Rather, the induced emf represents "work or energy per charge" "around and along a path".

# Lenz's Law

- When a changing magnetic flux induces a current, the induced current *itself* will create an *additional* magnetic field.
- The induced current will always produce a magnetic field that opposes the *change* in magnetic flux.
- If magnetic flux is increasing then the induced magnetic field will point opposite the original.
- This is an easier method for finding the sense of the emf than using the RHR and negative sign in Faraday's Law.



 $\oint \vec{E} \cdot d\vec{\ell} = -\frac{d}{dt} \int \vec{B} \cdot d\vec{A}$ 

The product of electric field and length of path is the same as that used to find a potential *difference* <u>between two points</u>. *However*, in this case it represents a *voltage "around"* a <u>closed path</u>. Is *this* electric field conservative?

### The Induced Electric Field

$$\oint \vec{E} \cdot d\vec{\ell} = -\frac{d}{dt} \int \vec{B} \cdot d\vec{A}$$

The electric field in *this* equation is an *induced* electric field and has different properties than a "regular" *electrostatic* field.

The induced electric field lines are continuous closed loops. This field can do work on charged particles that circulate along a loop.