

Rotational Mechanics Equations Comparison

Translation

position \vec{r}

velocity $\vec{v} = \frac{d\vec{r}}{dt}$

acceleration $\vec{a} = \frac{d\vec{v}}{dt}$

constant acceleration:

$$x = x_0 + v_0 t + \frac{1}{2} a t^2$$

$$v = v_0 + a t$$

$$v^2 = v_0^2 + 2a(x - x_0)$$

2nd Law $\Sigma \vec{F} = m\vec{a}$

mass m

force \vec{F}

work $W = \int \vec{F} \cdot d\vec{r}$

kinetic energy $K = \frac{1}{2} m v^2$

momentum $\vec{p} = m\vec{v}$

impulse $\vec{J} = \int \vec{F} dt = \Delta \vec{p}$

Rotation

angular position $\bar{\theta}$

angular velocity $\bar{\omega} = \frac{d\bar{\theta}}{dt}$

angular acceleration $\bar{\alpha} = \frac{d\bar{\omega}}{dt}$

constant angular acceleration:

$$\theta = \theta_0 + \omega_0 t + \frac{1}{2} \alpha t^2$$

$$\omega = \omega_0 + \alpha t$$

$$\omega^2 = \omega_0^2 + 2\alpha(\theta - \theta_0)$$

2nd Law $\Sigma \vec{\tau} = I\bar{\alpha}$

rotational inertia $I = \Sigma m_i r_i^2 = \int r^2 dm$
 $I = I_{CM} + Mh^2$

torque $\vec{\tau} = \vec{r} \times \vec{F} = r_{\perp} F = r F_{\perp}$

work $W = \int \vec{\tau} \cdot d\bar{\theta}$

kinetic energy $K = \frac{1}{2} I \omega^2$

angular momentum $\vec{L} = I\bar{\omega}$

angular impulse $\vec{A} = \int \vec{\tau} dt = \Delta \vec{L}$

“Linking” Equations

$$s = r\theta$$

$$v = r\omega$$

$$a_{\theta} = r\alpha$$

$$a_r = r\omega^2$$

$$\vec{\ell} = \vec{r} \times \vec{p} = r_{\perp} p = r p_{\perp}$$