## the Stars

I. Position and Motion Parallax, Proper Motion, Redshift
II. Size

Dwarfs, Giants, Stefan-Boltzman
III. Brightness

Magnitude, flux,
IV. Color
$B-V$ index
V. Spectral Type H-R diagrams

| The student will be able to: |  | HW: |
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| 13 | Describe and define the Hertzsprung-Russell diagram in terms of each axis. | 19-23 |
| 14 | Plot a star's coordinates on the H-R diagram. |  |
| 15 | Explain and illustrate how the H-R diagram is used to help classify and understand different types of stars such as main sequence stars, red giants, blue giants, supergiants, red dwarfs, and white dwarfs. |  |
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| 20 | Describe properties and significance of open clusters and globular clusters. |  |

# Parallax \& Proper Motion 

Where are the stars?
(and what are they doing?)
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## Parallax

- Parallax is a cyclical shift in a star's apparent position on the celestial sphere.
- A star that exhibits parallax appears to move and return to its starting point over the course of precisely one year.

Parallax Demonstrated

|  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

1. Close your left eye and use your right eye to line up your index finger with the zero.
2.Then, without moving your finger, close your right eye and open your left eye.
3.Repeat with your finger at a different distance in front of you - what happens to the amount of parallax?

## Two pictures taken from different locations - which object was closer to the camera?

## Telephone Pole

Lights

## Tree



## Two pictures taken from different locations

- which object was closer to the camera?

Telephone Pole
Lights


The distant mountains can be used as a reference and appear to not move at all.


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# Riäge $\overbrace{}^{\circ}$ Lights 

## The distant mountains can be used as a reference and appear to not move at all.

dge has the est shift and so her away than and the lights.


The pole was closest to the camera and appears shifted the most.
ens.

## Parallax Explained

- Parallax is a shift in apparent position due to the motion of Earth in its orbit.
- The amount of parallax depends upon the distance to the star. The greater the distance, the less the parallax.
- Put another way: the distance is inversely proportional to the parallax.
(a)



## Parallax

(b)

As seen in January
Over the course of a year a relatively nearby star will appear to move because of Earth's motion.
(a)


## Parallax

(b)

As seen in July

The effect is tiny, and was not observed or measured with certainty until the 1830's.

## Near Celestial Pole: <br> Near Ecliptic:



## Parallax Equation:

$$
d=\frac{1}{p}
$$

Where: $\quad d=$ distance in parsecs $p=$ parallactic angle in arc seconds

1. Star A has parallax $0.40^{\prime \prime}$. How far away is it?
2. Star B' s position shifts $0.20^{\prime \prime}$ east from January to July and 0.20" west from July to January. How far away is it?
3. Find the distance based on parallax: (a) Barnard's Star, (b) 61 Cygni, (c) Vega
4. Schedar and Caph ( $\alpha$ and $\beta$ Cass) are separated by $5.0^{\circ}$. But how far apart are they (really)? Parallaxes: 59.6 mas, 14.3 mas.
5. What should be the parallax of BI 253 given its distance is 50000 pc ?

## Measuring Parallactic Angles

- The greatest known parallax is $0.769^{\prime \prime}$, that of the star Proxima Centauri.
- This is a tiny, tiny angle!
- Parallax was first measured in the 1830' s by Bessel and Struve using telescopes designed and built by Fraunhofer.
- First stars for which parallax was measured: 61-Cygni, Vega, Alpha Centauri


## Measuring Parallactic Angles

- Using ground-based optics the smallest parallax measurable is about 0.03 ".
- Adaptive optics can push this to $0.01^{\prime \prime}$.
- The ESA satellite Hipparcos measured down to 0.005 " and catalogued about one million stars. (1989 thru 1993) The greatest detectable distance was about 200 pc. Fairly accurate to about 50 pc.
- Update: ESA Gaia can measure down to 0.000 024". Greatest detectable 40 kpc . Fairly accurate to about 10 kpc by 2020.


## Parallactic Angles - how small?

- A parallax of $0.772^{\prime \prime}$ is like a shift of 1 inch observed from 4.2 miles!
(Largest known - "easiest" to observe!)
- A parallax of $0.03^{\prime \prime}$ is like a shift of 1 inch observed from 100 miles!
(Ground-based limit)
- A parallax of $0.005^{\prime \prime}$ is like a shift of 1 inch observed from 600 miles!
(Hipparcos space-based limit)
- A parallax of 0.000024 " is like a shift of 1 inch observed from 140000 miles!
(Gaia space-based limit)


## Comprehending Astronomical Distances

- To help you understand how far away the stars are, consider a scale where 1 inch represents the distance from the Earth to the Sun.
- On this scale: 1 inch = 1 AU.
- Coincidentally, using the same scale: 1 mile = 1 light-year.
(The number of inches in a mile happens to be very nearly the same as the number of astronomical units in a light-year!)


## At this scale ( $1 \mathrm{in}=1 \mathrm{AU} ; 1 \mathrm{mi}=1 \mathrm{ly})$



At this scale the Sun would be only 0.01 inch in diameter (much smaller than shown here). At the same avg speed as the Apollo missions, it would take about 3 years to travel 1 AU .

震, At this scale ( $1 \mathrm{in}=1 \mathrm{AU} ; 1 \mathrm{mi}=1 \mathrm{ly}$ ), there are no stars nearer than this circle!


Note: at this scale, the speed of light is about that of a slow snail ( 0.00011 mph ).






$$
1000 \text { pc }
$$

Essentially all 6000 stars visible to the naked eye are within this region!

## The Milky Way Galaxy

## 1000 pc


observation shadow of galactic core

## Astronomical Distances

- The astronomical unit (radius of Earth' s orbit):

1 A.U. $=1.496 \times 10^{11} \mathrm{~m}$

- The light-year (distance light travels in 1 year):
$1 \mathrm{ly}=63240$ A.U. $=9.46 \times 10^{15} \mathrm{~m}$
- The parsec (distance to star with parallax of $1^{\prime \prime}$ ):

$$
1 \mathrm{pc}=3.26 \mathrm{ly}=206265 \mathrm{~A} . \mathrm{U} .=3.09 \times 10^{16} \mathrm{~m}
$$

| Name of star | Parallax <br> $(\operatorname{arc~sec})$ | Distance <br> $(\mathrm{pc})$ | Distance <br> $(\mathrm{ly})$ | Distance <br> $(\mathrm{m})$ |
| :---: | :---: | :---: | :---: | :---: |
| Barnard' s Star | 0.545 |  |  |  |
| Vega | 0.13 |  |  |  |
| Sirius |  | 2.7 |  |  |
| Alpha Centauri |  | 1.33 |  |  |
| Proxima Centauri |  |  | 4.24 |  |
| Rigel |  |  | 815 |  |
| Deneb |  |  |  | $1.33 \times 10^{19}$ |
| Capella |  |  |  | $4.32 \times 10^{17}$ |


| Name of star | Parallax <br> $($ arc sec $)$ | Distance <br> $(\mathrm{pc})$ | Distance <br> $(\mathrm{ly})$ | Distance <br> $(\mathrm{m})$ |
| :---: | :---: | :---: | :---: | :---: |
| Barnard's star | 0.545 | 1.83 | 5.98 | $5.66 \times 10^{16}$ |
| Vega | 0.13 | 7.7 | 25 | $2.4 \times 10^{17}$ |
| Sirius | 0.37 | 2.7 | 8.8 | $8.3 \times 10^{16}$ |
| Alpha Centauri | 0.752 | 1.33 | 4.34 | $4.10 \times 10^{16}$ |
| Proxima Centauri | 0.769 | 1.30 | 4.24 | $4.01 \times 10^{16}$ |
| Rigel | 0.0040 | 250 | 815 | $7.7 \times 10^{18}$ |
| Deneb | 0.0023 | 431 | 1410 | $1.33 \times 10^{19}$ |
| Capella | 0.0714 | 14.0 | 45.7 | $4.32 \times 10^{17}$ |

## Stellar Aberration

- Aberration is also a cyclical apparent change in the position of stars.
- However, ALL stars in a particular region of the sky undergo the same shift over the course of one year.
- Aberration does not tell us anything about the star (but rather relates to Earth's velocity in its orbit).


The star appears to be in a different location.

Because it is moving, a telescope must be pointed in a slightly "tilted" direction in order for light to pass from one end to the other.


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## Parallax vs. Aberration

- Stellar aberration is a much larger shift of around $20^{\prime \prime}$ and was discovered by Bradley in the 1720's.
- Unlike parallax, aberration is unrelated to distance - near stars and far stars exhibit the same aberration.
- Unlike parallax, the shift is in the same direction as Earth's motion, instead of the opposite!

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## Proper Motion

- Proper Motion is a steady shift in a star's apparent position on the celestial sphere.
- The star moves steadily in a particular direction and does not return to its starting point.


## Barnard' s Star 20 years of Proper Motion:



By Steve Quirk [Public domain], via Wikimedia Commons

## Proper Motion Explained

- Proper Motion is a change due to actual motion of a star through space.
- The amount depends on how fast the star is moving, the direction the star is moving, and the distance to the star.
- 61-Cygni is known as the "Flying Star" exhibits a large proper motion of about 6 arcseconds per year.


## Suppose a star is moving through space . . .

Earth
Star

From our perspective on Earth it will change position by a certain angle. This angle is the "proper motion" and is usually given in arc seconds per year.

Earth
Star

From our perspective on Earth it will change position by a certain angle. This angle is the "proper motion" and is usually given in arc seconds per year.

Angle in arc sec

Earth
Star

Note that two different stars could have the same proper motion in spite of very different actual motion in space ...


Earth
Two Stars

Also two different stars could have the same actual motion in space and very different proper motion from Earth ...


Earth
Two Stars

The overall velocity through space is a combination of "radial velocity" and "transverse velocity".


Earth

Radial velocity can be determined by the doppler shift.

Transverse velocity can be determined by proper motion.


Earth

# The overall velocity can then be found by the Pythagorean Theorem: 

$$
v^{2}=v_{r}^{2}+v_{t}^{2}
$$



Earth

## Stellar Motion Practice

5. Proxima Centauri has transverse velocity 23.8 $\mathrm{km} / \mathrm{s}$ and radial velocity $-22.2 \mathrm{~km} / \mathrm{s}$. Find its true velocity through space. Will it get even closer to us?
6. Canopus: $v_{\mathrm{t}}=2.9 \mathrm{~km} / \mathrm{s}$ and $v_{\mathrm{r}}=+20.3 \mathrm{~km} / \mathrm{s}$. Find its true velocity through space. Where is it going?
7. Scholz's star has parallax $0.147^{\prime \prime}$ and proper motion $0.12^{\prime \prime} / \mathrm{yr}$. The wavelengths of its light are shifted: $\Delta \lambda / \lambda=+2.75 \times 10^{-4}$. Find its velocity. Where has it been?

## Gliese 710 - the "Death Star"?

- parallax $=0.05252^{\prime \prime}$
- proper motion $=0.461 \mathrm{mas} / \mathrm{yr}$
- $\Delta \lambda / \lambda=-4.84 \times 10^{-5}$
- $m=9.69$
- Based on this information it is predicted that this star will ...?


## Gliese 710 - the "Death Star"?

- parallax = 0.05252"
- proper motion $=0.461 \mathrm{mas} / \mathrm{yr}$
- $\Delta \lambda / \lambda=-4.84 \times 10^{-5}$
- $m=9.69$
- Based on this information it is predicted that this star will pass within 0.06 pc of the Sun in about one million years. It will appear as bright as Betelgeuse!
- Compare and contrast with Scholz's star...

